

නව නිර්දේශය/புதிய பாடத்திட்டம் / New Syllabus

NEW

ශ්‍රී ලංකා විභාග දෙපාර්තමේන්තුව ශ්‍රී ලංකා විභාග දෙපාර්තමේන්තුව ශ්‍රී ලංකා විභාග දෙපාර්තමේන්තුව ශ්‍රී ලංකා විභාග දෙපාර්තමේන්තුව ශ්‍රී ලංකා විභාග දෙපාර්තමේන්තුව
 திணைக்களம் இலங்கைப் பரீட்சைத் திணைக்களம் இலங்கைப் பரීட்சைத் திணைக்களம் இலங்கைப் பரීட்சைத் திணைக்களம் இலங்கைப் பரීட்சைத் திணைக்களம்
 Department of Examinations, Sri Lanka Department of Examinations, Sri Lanka Department of Examinations, Sri Lanka Department of Examinations, Sri Lanka Department of Examinations, Sri Lanka
 இலங்கைப் பரීட்சைத் திணைக்களம் இலங்கைப் பரීட்சைத் திணைக்களம் இலங்கைப் பரීட்சைத் திணைக்களம் இலங்கைப் பரීட்சைத் திணைக்களம் இலங்கைப் பரීட்சைத் திணைக்களம்

අධ්‍යයන පොදු සහකීය පත්‍ර (උසස් පෙළ) විභාගය, 2020
 கல்விப் பொதுத் தராதரப் பத்திர (உயர் தர)ப் பரீட்சை, 2020
 General Certificate of Education (Adv. Level) Examination, 2020

ගණිතය II
 கணிதம் II
 Mathematics II

07 E II

පැය තුනයි
 மூன்று மணித்தியாலம்
 Three hours

අමතර කියවීමේ කාලය - මිනිත්තු 10 යි
 மேலதிக வாசிப்பு நேரம் - 10 நிமிடங்கள்
 Additional Reading Time - 10 minutes

Use additional reading time to go through the question paper, select the questions you will answer and decide which of them you will prioritise.

Index Number

Instructions:

- * This question paper consists of two parts;
 Part A (Questions 1–10) and Part B (Questions 11–17).
Part A:
 Answer all questions. Write your answers to each question in the space provided. You may use additional sheets if more space is needed.
- Part B:**
 Answer five questions only. Write your answers on the sheets provided.
- * At the end of the time allotted, tie the answer scripts of the two parts together so that Part A is on top of Part B and hand them over to the supervisor.
- * You are permitted to remove **only Part B** of the question paper from the Examination Hall.
- * Statistical tables will be provided.

For Examiners' Use only

(07) Mathematics II		
Part	Question No.	Marks
A	1	
	2	
	3	
	4	
	5	
	6	
	7	
	8	
	9	
	10	
B	11	
	12	
	13	
	14	
	15	
	16	
	17	
	Total	

Total

In Numbers	
In Words	

Code Numbers

Marking Examiner	
Checked by:	1
	2
Supervised by:	

கிடைக்காத அனைத்து உரிமைகளும் பதிப்பரிமையுடையது / All Rights Reserved

නව නිර්දේශය / புதிய பாடத்திட்டம் / New Syllabus

இலங்கை பரீட்சைத் திணைக்களம் இலங்கைப் பரீட்சைத் திணைக்களம் இலங்கைப் பரீட்சைத் திணைக்களம் இலங்கைப் பரீட்சைத் திணைக்களம் இலங்கைப் பரீட்சைத் திணைக்களம்
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 கல்விப் பொதுத் தராதரப் பத்திர (உயர் தர)ப் பரீட்சை, 2020
 General Certificate of Education (Adv. Level) Examination, 2020

ගණිතය II
 கணிதம் II
 Mathematics II

07 E II

Part B

* Answer five questions only.

11. A factory manufactures tables and chairs. The production of each item requires three operations: cutting, assembling and finishing.

For cutting, assembling and finishing, the maximum number of hours that can be used are 600, 160 and 280, respectively. The following table gives the number of hours required for each operation in producing each item and the profit per item sold.

	Number of hours for cutting	Number of hours for assembling	Number of hours for finishing	Profit (in thousands of rupees)
Table	5	1	1	12
Chair	6	2	4	15

The factory wishes to maximize the profit.

- Formulate this as a linear programming problem.
- Sketch the feasible region.
- Using the graphical method, find the solution of the problem formulated in part (i) above.
- Due to shortage of storage space, the factory has to limit the total number of tables and chairs produced to at most 108. Find the decrease in the profit due to above limitation, if the factory still wishes to maximize the profit.

12.(a) Let $A = \begin{pmatrix} 4 & 7 \\ -1 & -2 \end{pmatrix}$. Write down A^{-1} .

Let $B = \begin{pmatrix} -1 & 3 \\ 0 & 1 \end{pmatrix}$.

Find the matrix C such that $AC = B$ and show that

$$AC - CA = \begin{pmatrix} 20 & 43 \\ -11 & -20 \end{pmatrix}.$$

Find the matrix D such that $AC - DA = O$, where O is the zero matrix of order 2.

(b) Let $a \in \mathbb{R}$. Write the pair of simultaneous equations

$$(a - 5)x + 3y = a$$

$$-4x + (a + 2)y = 1$$

in the form $\mathbf{PX} = \mathbf{Q}$, where $\mathbf{X} = \begin{pmatrix} x \\ y \end{pmatrix}$, and \mathbf{P} and \mathbf{Q} are matrices to be determined.

Express $\Delta = \begin{vmatrix} (a-5) & 3 \\ -4 & (a+2) \end{vmatrix}$ as a quadratic function of a .

Show that the roots of the equation $\Delta = 0$ are $a = 1$ and $a = 2$.

Show that the above pair of equations has

- (i) infinitely many solutions when $a = 1$,
- (ii) no solution when $a = 2$,
- (iii) a unique solution when $a = 3$.

13.(a) An unbiased cubic die with faces marked 1, 2, 2, 3, 3, 4 is tossed twice. Let A be the event that the sum of the numbers obtained is 4 and B be the event that the sum of the numbers obtained is even.

Find $P(A)$, $P(B)$ and $P(A|B)$.

(b) Four digits from the set of digits $\{1, 2, 3, 4, 5, 6\}$ are chosen without replacement and a 4-digit number is made.

- (i) How many different 4-digit numbers can be made?
- (ii) How many of these 4-digit numbers start with 3 or 5?

(c) A team of four people must be selected from a group of four males and two females.

- (i) How many different teams of four people can be selected?
- (ii) Find the probability that both females are selected to these teams.

14. A box X contains 4 red cards and 6 blue cards. A box Y contains 3 red cards and 2 blue cards. A biased coin with $\frac{2}{3}$ as the probability of getting a head is tossed. If the outcome is a head, 2 cards are drawn from the box X , at random without replacement, and if it is a tail, 2 cards are drawn from the box Y , at random without replacement. Find the probability that

- (i) both cards drawn are red,
- (ii) at least one of the cards drawn is red,
- (iii) the two cards drawn are of different colours,
- (iv) the two cards drawn are of different colours, given that at least one of the cards drawn is red.

- 15.(a) The time X , measured in minutes, between consecutive arrivals of buses to a certain bus stop is exponentially distributed with probability density function

$$f(x) = \begin{cases} \lambda e^{-\lambda x} & , x > 0, \\ 0 & , \text{otherwise,} \end{cases}$$

where $\lambda (> 0)$ is a parameter.

If the mean number of buses that arrive at the bus stop in an hour is 12, find the value of λ .

- (i) After a bus arrives at the bus stop, find the probability that the time taken for the next bus to arrive at the bus stop is
- (α) between one minute to three minutes,
 (β) less than five minutes.
- (ii) If it is given that five minutes has already passed from the arrival of a bus to the bus stop, find the probability that it takes at least an additional two minutes for the next bus to arrive.
- (b) A continuous random variable X is uniformly distributed over the interval $[a, b]$.
 Find the values of a and b such that $P(X < 16) = 0.4$ and $P(X > 21) = 0.2$.

16. Hundred students faced an entrance test. The frequency distribution of the marks they obtained is given in the following table:

Marks	frequency
0 – 20	15
20 – 40	20
40 – 60	40
60 – 80	15
80 – 100	10

- (i) Estimate each of the following:
- (a) the mean,
 (b) the standard deviation,
 (c) the median,
 (d) the inter quartile range and
 (e) the mode
 of the marks.
- (ii) After rescrutiny, it was discovered that the marks of two answer scripts should be changed as follows:

Marks before rescrutiny	Marks after rescrutiny
50	62
70	75

Find the mean of the new distribution of marks.

17. The duration of activities of a project and the flow of activities are given in the following table:

Activity	Preceding Activity (Activities)	Duration (in Weeks)
A	–	03
B	A	08
C	A	05
D	A	03
E	B	06
F	C	03
G	E, F	04
H	D, F	06
I	G, H	03

- (i) Construct the project network.
- (ii) Prepare an activity schedule that includes earliest start time, earliest finish time, latest start time, latest finish time and float for each activity.
- (iii) Find the total duration of the project.
- (iv) What are the activities that can be delayed without extending the total duration of the project?
- (v) Write down the critical path of this project.
- (vi) Suppose that the duration of the activity D has to be extended by two weeks due to an unexpected matter. Determine whether the project could still be completed within the total duration calculated in part (iii) above.

* * *