ිසියලු ම හිමිකම් ඇවිරිණි / ලාඟුට පුනිට්පුහිඟෙපාළා / All Rights Reserved]

(නව නිර්දේශය/பුනිய பாடத்திட்டம்/New Syllabus

g ean gang centrogodope ලී ලංකා විභාග දෙපාර්ත**ිල් ලින්න විභාග සහ**ජ්ය මෙන්න විභාග දෙපාර්තමේත්තුව ලී ලංකා විභාග දෙපාර්තමේත්තුව නිශාක්ෂියක්ව ඉහිතින් අත්තිය විභාග දෙපාර්තමේත්තුව ලී ලංකා විභාග දෙපාර්තමේත්තුව ලේකා දෙපාර්තමේත්තුව ලී ලංකා විභාග දෙපාර්තමේත්තුව ලේකා දෙපාර්තමේත්තුව ලේකා දින්න දෙපාර්තමේත්තුව ලේකා විභාග දෙපාර්තමේත්තුව ලේකා දෙපාර්තමේත්තුව ලේකා විභාග දෙපාර්තමේත්තුව ලේකා විභාග දෙපාර්තමේත්තුව ලේකා විභාග දෙපාර්තමේත්තුව ලේකා විභාග දෙපාර්තමේත්තුව ලේකා දෙපාර්තමේත්තුව ලේකා විභාග ද

සංයුක්ත ගණිතය II இකணந்த සணிதம் II Combined Mathematics II



சැය තුනයි மூன்று மணித்தியாலம் **Three hours** අමතර කියවීම් කාලය - මිනිත්තු 10 යි மேலதிக வாசிப்பு நேரம் - 10 நிமிடங்கள் Additional Reading Time - 10 minutes

Use additional reading time to go through the question paper, select the questions you will answer and decide which of them you will prioritise.

Index Number

Instructions:

- * This question paper consists of two parts;
 - Part A (Questions 1-10) and Part B (Questions 11-17)
- * Part A:
 - Answer all questions. Write your answers to each question in the space provided. You may use additional sheets if more space is needed.
- * Part B:
 - Answer five questions only. Write your answers on the sheets provided.
- * At the end of the time allotted, tie the answer scripts of the two parts together so that $\mathbf{Part}\ \mathbf{A}$ is on top of $\mathbf{Part}\ \mathbf{B}$ and hand them over to the supervisor.
- * You are permitted to remove only Part B of the question paper from the Examination Hall.
- * In this question paper, g denotes the acceleration due to gravity.

For Examiners' Use only

(10) Combined Mathematics II		
Part	Question No.	Marks
	1	
	2	
	3	
	4	
A	5	
	6	
	7	
	8	
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(10) Combined Mathematica II

	Total	
In Numbers		
In Words		

Code Numbers

Marking Examiner

Checked by:

2

Supervised by:

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1.	Two particles A and B each of mass m , moving in the same straight line on a smooth horizonta	Time to the same t
	floor, but in opposite directions collide directly. The velocities of A and B just before collision are	
	u and λu , respectively. The coefficient of restitution between A and B is $\frac{1}{2}$.	
	A Find the velocity of A just after collision and show that if $\lambda > \frac{1}{3}$, then	1
	(m) $\stackrel{u}{\longrightarrow}$ $\stackrel{\lambda u}{\longleftarrow}$ $\stackrel{\lambda u}{\longleftarrow}$ the direction of motion of A is reversed.	
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of o	A particle is projected from a point O on a horizontal floor	and the same
y = 0	A particle is projected from a point O on a horizontal floor with initial velocity $u = \sqrt{2ga}$ and at an angle $\alpha \left(0 < \alpha < \frac{\pi}{2}\right)$ to	PHILIPPINE TO THE PROPERTY OF
y = 0	with initial velocity $u = \sqrt{2ga}$ and at an angle $\alpha \left(0 < \alpha < \frac{\pi}{2}\right)$ to	
y d 0	with initial velocity $u = \sqrt{2ga}$ and at an angle $\alpha \left(0 < \alpha < \frac{\pi}{2}\right)$ to the horizontal. The particle just clears a vertical wall of height	
y al o	with initial velocity $u = \sqrt{2ga}$ and at an angle $\alpha \left(0 < \alpha < \frac{\pi}{2}\right)$ to the horizontal. The particle just clears a vertical wall of height	
, , ,	with initial velocity $u = \sqrt{2ga}$ and at an angle $\alpha \left(0 < \alpha < \frac{\pi}{2}\right)$ to the horizontal. The particle just clears a vertical wall of height $\frac{3a}{4}$ located at a horizontal distance a from O . Show that $\sec^2\alpha - 4\tan\alpha + 3 = 0$.	
y d o	with initial velocity $u = \sqrt{2ga}$ and at an angle $\alpha \left(0 < \alpha < \frac{\pi}{2}\right)$ to the horizontal. The particle just clears a vertical wall of height $\frac{3a}{4}$ located at a horizontal distance α from O . $u = \sqrt{2ga}$	
y # # 0	with initial velocity $u = \sqrt{2ga}$ and at an angle $\alpha \left(0 < \alpha < \frac{\pi}{2}\right)$ to the horizontal. The particle just clears a vertical wall of height $\frac{3a}{4}$ located at a horizontal distance a from O . Show that $\sec^2\alpha - 4\tan\alpha + 3 = 0$.	
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940	with initial velocity $u = \sqrt{2ga}$ and at an angle $\alpha \left(0 < \alpha < \frac{\pi}{2}\right)$ to the horizontal. The particle just clears a vertical wall of height $\frac{3a}{4}$ located at a horizontal distance a from O . Show that $\sec^2\alpha - 4\tan\alpha + 3 = 0$.	
2 0	with initial velocity $u = \sqrt{2ga}$ and at an angle $\alpha \left(0 < \alpha < \frac{\pi}{2}\right)$ to the horizontal. The particle just clears a vertical wall of height $\frac{3a}{4}$ located at a horizontal distance a from O . Show that $\sec^2\alpha - 4\tan\alpha + 3 = 0$.	
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3.	Two particles A and B , each of mass m , attached to the two ends of a light inextensible string which passes over a fixed smooth pulley are in equilibrium with the particle A at a height a from a horizontal floor and the particle B touching the floor, as shown in the figure. Now, the particle A is given an impulse mu vertically downwards. Find the velocity of the particle A just after the impulse. Write down the time taken by A to reach the floor.	$A \circ \overline{A}$
		$B \bigcirc$
		<i>DO</i> 4
	.3	
4.	A car of mass 1500 kg travels on a straight horizontal road against a constant resistar 500 N. Find the acceleration of the car when the engine of the car is working at per the car is travelling with speed 25 m s ⁻¹ . At this instant, the engine of the car is turned off. Find the speed of the car after the instant the engine was turned off.	ower 50 kW and
4.	500 N. Find the acceleration of the car when the engine of the car is working at per the car is travelling with speed 25 m s ⁻¹ . At this instant, the engine of the car is turned off. Find the speed of the car after	ower 50 kW and
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5	3. A particle P of mass $2m$, hanging freely from a horizontal ceiling
	by a light inextensible string of length l , is in equilibrium. Another
	particle of mass m moving in a horizontal direction with velocity u
	collides with the particle P and coalesces to it. The string remains
	taut after the collision and the composite particle just reaches the $u m 2m$
	ceiling. Show that $u = \sqrt{18gl}$.
	\$
	Let $\alpha > 0$ and in the usual notation, let $\mathbf{i} + \alpha \mathbf{j}$ and $\alpha \mathbf{i} - 2 \mathbf{j}$ be the position vectors of two points
	A and B, respectively, with respect to a fixed origin O. Also, let C be the point on AB such that
	$AC: CB = 1:2$. It is given that OC is perpendicular to AB . Find the value of α .

7.	A uniform rod ACB of length $2a$ and weight W is kept in equilibrium with the end A against a smooth vertical wall by a smooth peg placed at C , as shown in the figure. It is given that the reaction at A from the wall is $\frac{W}{\sqrt{3}}$. Show that the angle α that the rod makes with the horizontal is $\frac{\pi}{6}$.
	Show also that $AC = \frac{3}{4}a$.
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8.	A small bead of weight W is threaded to a fixed rough straight wire inclined at an angle $\frac{\pi}{4}$ to the horizontal. The bead is kept in equilibrium by a horizontal force of magnitude P as shown in the figure. The coefficient of friction between the bead and the wire is $\frac{1}{2}$. Obtain equations sufficient to determine the frictional force F and the normal reaction R on the bead, in terms of P and W . It is given that $\frac{F}{R} = \frac{W - P}{W + P}$. Show that $\frac{W}{3} \le P \le 3W$.
8.	an angle $\frac{\pi}{4}$ to the horizontal. The bead is kept in equilibrium by a horizontal force of magnitude P as shown in the figure. The coefficient of friction between the bead and the wire is $\frac{1}{2}$. Obtain equations sufficient to determine the frictional force F and the normal reaction R on the bead, in terms of P and W .
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9.	Let A and B be two events of a sample space Ω . In the usual notation, it is given th	ıat
	$P(A) = \frac{3}{5}$, $P(B \mid A) = \frac{1}{4}$ and $P(A \cup B) = \frac{4}{5}$. Find $P(B)$.	
	Show that the events A and B are not independent.	
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10.	A set of 5 observations of positive integers, each less than or equal to 10, has mean, media and mode each equals to 6. The range of the observations is 9. Find these five observations.	- 1
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(නව නිර්දේශය/பුதிய பாடத்திட்டம்/New Syllabus)

ந்தை நேறு நேறு நேறு நிறை செறுப்படு இது நிறை செறுப்படு இது நிறு செறுப்படு இது நிறை செறுப்படுக்கு நிறைக்களம் இலங்கைப் படிக்கத் நிறைக்களம் இலங்கைப் படிக்கத் நிறைக்களம் இலங்கைப் படிக்கத் நிறைக்களம் நிறைக்களம்

අධානයන පොදු සහතික පතු (උසස් පෙළ) විභාගය, 2020 கல்விப் பொதுத் தராதரப் பத்திர (உயர் தர)ப் பரீட்சை, 2020 General Certificate of Education (Adv. Level) Examination, 2020

සංයුක්ත ගණිතය II இഞைந்த கணிதம் II Combined Mathematics II

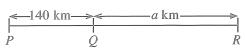


Part B

* Answer five questions only.

(In this question paper, g denotes the acceleration due to gravity.)

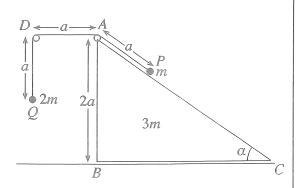
11.(a) Three railway stations P, Q and R located in a straight line such that PQ = 140 km and QR = a km, as shown in the figure. At time t = 0, a train A starts from rest



at P and moves towards Q with constant acceleration $f \, \mathrm{km} \, \mathrm{h}^{-2}$ for half an hour and maintains the velocity it had at time $t = \frac{1}{2} \, \mathrm{h}$ for three hours. Then it moves with constant retardation $f \, \mathrm{km} \, \mathrm{h}^{-2}$ and comes to rest at Q. At time $t = 1 \, \mathrm{h}$, another train B starts from rest at R and moves towards Q with constant acceleration $2f \, \mathrm{km} \, \mathrm{h}^{-2}$ for T hours and then with a constant retardation $f \, \mathrm{km} \, \mathrm{h}^{-2}$ and comes to rest at Q. Both trains come to rest at the same instant. Sketch velocity-time graphs for the motions of A and B in the same diagram.

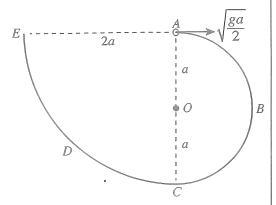
Hence or otherwise, show that f = 80 and find the values of T and a.

- (b) A ship is sailing due west with uniform speed u relative to earth and a boat is sailing in a straight line path with uniform speed $\frac{u}{2}$ relative to earth. At a certain instant, the ship is at a distance d at an angle $\frac{\pi}{3}$ east of north from the boat.
 - (i) If the boat is sailing relative to earth in the direction making an angle $\frac{\pi}{6}$ west of north, show that the boat can intercept the ship and that the time taken by the boat to intercept the ship is $\frac{2d}{\sqrt{3}u}$.
 - (ii) If the boat is sailing relative to earth in the direction making an angle $\frac{\pi}{6}$ east of north, show that the speed of the boat relative to the ship is $\frac{\sqrt{7}u}{2}$ and that the shortest distance between the ship and the boat is $\frac{d}{2\sqrt{7}}$.
- 12.(a) The triangle ABC in the figure is the vertical cross-section through the centre of gravity of a smooth uniform wedge of mass 3m with $A\hat{C}B = \alpha$, $A\hat{B}C = \frac{\pi}{2}$ and AB = 2a such that the face containing BC is placed on a smooth horizontal floor. The line AC is a line of greatest slope of the face containing it. The point D is a fixed point in the plane of ABC such that AD is horizontal. Two particles P and Q of masses m and 2m, respectively



are attached to the two ends of a light inextensible string of length 3a passing over smooth small pulleys fixed at A and D. The system is released from rest with the particle P held on AC and the particle Q hanging freely such that AP = AD = DQ = a, as shown in the figure. Obtain equations sufficient to determine the time taken by the particle Q to reach the floor.

(b) A smooth thin wire ABCDE is fixed in a vertical plane, as shown in the figure. The portion ABC is a semicircle with centre O and radius a, and the portion CDE is a quarter of a circle with centre A and radius 2a. The points A and C lie on the vertical line through O and the line AE is horizontal. A small smooth bead P of mass m is placed at A and is given a velocity $\sqrt{\frac{ga}{2}}$ horizontally, and begins to move along the wire.

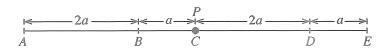


Show that the speed v of the bead P when \overrightarrow{OP} makes an angle θ ($0 \le \theta \le \pi$) with \overrightarrow{OA} is given by $v^2 = \frac{ga}{2}(5 - 4\cos\theta)$.

Find the reaction on the bead P from the wire at the above position and show that it changes its direction when the bead P passes the point $\theta = \cos^{-1}\left(\frac{5}{6}\right)$.

Write down the velocity of the bead P just before it leaves the wire at E and find the reaction on the bead P from the wire at that instant.

13. The points A, B, C, D and E lie on a straight line in that order, on a smooth horizontal table such that AB = 2a, BC = a, CD = 2a and DE = a, as



shown in the figure. One end of a light elastic string of natural length 2a and modulus of elasticity kmg is attached to the point A and the other end to a particle P of mass m. One end of another light elastic string of natural length a and modulus of elasticity mg is attached to the point E and the other end to the particle P. When the particle P is held at C and released, it stays in equilibrium. Find the value of k.

Now, the string AP is pulled until the particle P reaches the point D and released from rest. Show that the equation of motion of P from D to B is given by $\ddot{x} + \frac{3g}{a}x = 0$, where CP = x.

Using the formula $\dot{x}^2 = \frac{3g}{a}(c^2 - x^2)$, where c is the amplitude, show that the velocity of particle P when it reaches B is $3\sqrt{ga}$.

An impulse is given to the particle P when it reaches B so that the velocity of P just after the impulse is \sqrt{ag} in the direction of \overrightarrow{BA} .

Show that the equation of motion of P after passing B until it comes to instantaneous rest is given by $\ddot{y} + \frac{g}{a}y = 0$, where DP = y.

Show that the total time taken by the particle P, started at D, to reach B for the second time is $2\sqrt{\frac{a}{g}}\left(\frac{\pi}{3\sqrt{3}}+\cos^{-1}\left(\frac{3}{\sqrt{10}}\right)\right)$.

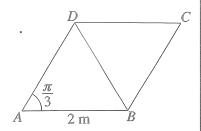
14. (a) Let a and b be two unit vectors.

The position vectors of three points \overrightarrow{A} , \overrightarrow{B} and \overrightarrow{C} with respect to an origin O, are 12a, 18b and 10a + 3b respectively. Express \overrightarrow{AC} and \overrightarrow{CB} in terms of a and b.

Deduce that A, B and C are collinear and find AC : CB.

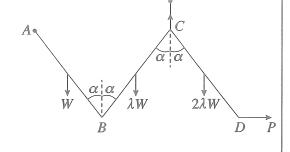
It is given that $OC = \sqrt{139}$. Show that $A\hat{O}B = \frac{\pi}{3}$.

(b) Let ABCD be a rhombus with AB = 2 m and $B\hat{A}D = \frac{\pi}{3}$. Forces of magnitude 10 N, 2 N, 6 N, P N and Q N act along AD, BA, BD, DC and CB respectively, in the directions indicated by the order of the letters. It is given that the resultant force is of magnitude 10 N and its direction is in the direction parallel to BC in the sense from B to C. Find the values of P and Q. Also, find the distance from A to the point where the line of action of the resultant force meets BA produced.



Now, a couple of moment M Nm acting in the counterclockwise sense and two forces, each of magnitude F N acting along CB and DC in the directions indicated by the order of the letters, are added to the system so that the resultant force passes through the points A and C. Find the values of F and M.

15.(a) Three uniform rods AB, BC and CD, each of length 2a are smoothly joined at the ends B and C. The weights of the rods AB, BC and CD are W, λW and 2λW, respectively. The end A is smoothly hinged to a fixed point. The rods are kept in equilibrium in a vertical plane by a light inextensible string attached to the joint C and to a fixed point vertically above C and by a horizontal force P applied to the end D such that A and C are at the same horizontal



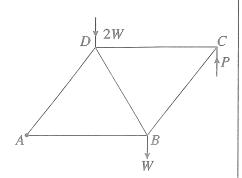
level and each of the rods making an angle α with the vertical, as shown in the figure. Show that $\lambda = \frac{1}{3}$.

Show also that the horizontal and vertical components of the force exerted on AB by CB at B are $\frac{W}{3}\tan\alpha$ and $\frac{W}{6}$, respectively.

(b) The framework shown in the adjoining figure is made from light rods AB, BC, CD, DA and BD, each of length 2a, freely jointed at A, B, C and D. There are loads of W and 2W at B and D, respectively. The framework is smoothly hinged at A to a fixed point and kept in equilibrium with AB horizontal by a vertical force P applied to it at C, as shown in the figure. Find the value of P in terms of W.

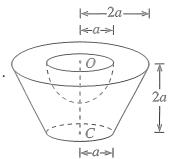
value of P in terms of W.

Draw a stress diagram using Bow's notation and hence, find the stresses in the rods stating whether they are tensions or thrusts.

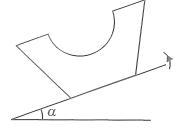


- 16. Show that the centre of mass of
 - (i) a uniform solid right circular cone of base radius r and height h is at a distance $\frac{h}{4}$ from the centre of the base,
 - (ii) a uniform solid hemisphere of radius r is at a distance $\frac{3r}{8}$ from its centre.

The adjoining figure shows a mortar S made by removing a solid hemisphere from a frustum of a solid uniform right circular cone having base radius 2a and height 4a. The radius and the centre of the upper circular face of the frustum are 2a and O, respectively, and those for the lower circular face are a and C, respectively. The height of the frustum is 2a. The radius and the centre of the removed solid hemisphere are a and O, respectively. Show that the centre of mass of mortar S lies at a distance $\frac{41}{48}a$ from O.



Mortar S is placed on a rough horizontal plane with its lower circular face touching the plane. Now, the plane is tilted upwards slowly. The coefficient of friction between the mortar and the plane is 0.9. Show that if $\alpha < \tan^{-1}(0.9)$, then the mortar stays in equilibrium, where α is the inclination of the plane to the horizontal.



17.(a) In a certain factory, machine A makes 50% of the items and the rest are made by machines B and C. It is known that 1%, 3% and 2% of the items made by A, B and C respectively are defective. The probability that a randomly selected item is defective is given to be 0.018. Find the percentages of items made by the machines B and C.

Given that a randomly selected item is defective, find the probability that it was made by the machine A.

(b) The time taken (in minutes) to travel to work from their homes of 100 employees of a certain factory are given in the following table:

Time taken	Number of employees
0 – 20	10
20 – 40	30
40 – 60	40
60 - 80	10
80 – 100	10

Estimate the mean, standard deviation and the mode of the distribution given above.

Later, all of the employees in the class interval 80-100 moved closer to the factory. It has changed the frequency of the class interval 80-100 from 10 to 0 and the frequency of the class interval 0-20 from 10 to 20.

Estimate the mean, standard deviation and the mode of the new distribution.