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තාමේන්තුව ලි ලංකා විභාග දෙපාර්**ලි අවරකාවේහාග දෙපාර්තමේන්තුව**ගග දෙපාර්තමේන්තුව ලී ලංකා විභාග දෙපාර්තමේන්තුව නියාක්ෂය සහ ඉහළ සහ අදිස් නියාක්ෂය සහ ations, Sri Lanka Department of Examinations, Sri Lanka Department of Examinat

ගණිතය II සණෝதம் II Mathematics II



පැය තුනයි

மூன்று மணித்தியாலம்

Three hours

අමතර කියවීම් කාලය - මිනිත්තු 10 යි மேலதிக வாசிப்பு நேரம் - 10 நிமிடங்கள் Additional Reading Time - 10 minutes

Use additional reading time to go through the question paper, select the questions you will answer and decide which of them you will prioritise.

Instructions:

* This question paper consists of two parts;

Part A (Questions 1-10) and Part B (Questions 11-17).

Part A:

Answer all questions. Write your answers to each question in the space provided. You may use additional sheets if more space is needed.

Part B:

Answer five questions only. Write your answers on the sheets provided.

- * At the end of the time allotted, tie the answer scripts of the two parts together so that Part A is on top of Part B and hand them over to the supervisor.
- * You are permitted to remove only Part B of the question paper from the Examination Hall.
- * Statistical tables will be provided.

For Examiners' Use only

	(07) Mathemati	cs II
Part	Question No.	Marks
	1	
	2	
	3	
	4	
A	5	
	6	
	7	
	8	
	9	
	10	
	11	
	12	
TD.	13	
В	14	
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	17	
	Total	

	Total
In Numbers	
In Words	

		Code Numbers
Marking Exami	ner	
Checked by:	1	
Chocked by.	2	
Supervised by:		

Part A

1.	Let a, b, c				
	:	а	а	2a+b+c	
	Show that	b	a+2b+c	b	$=-2(a+b+c)^3.$
		a+b+2c	С	С	$=-2(a+b+c)^3$.
		• • • • • • • • • • • • • • • • • • • •	• • • • • • • • • • • • • • • • • • • •	• • • • • • • • • • • • • • • • • • • •	
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<i>'</i>	Verify that		\		$\mathbf{C} = \begin{pmatrix} -1 & 0 \\ 1 & 3 \end{pmatrix}. $ Find AB and BC .
		~ ~ 0 0 0 0 0 0 0 0 0 0 0 0			
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Index No.:

3.	The mean and the standard deviation of a set of 10 observations are 5 and 10, respectively. Find the sum and the sum of squares of these observations. If another observation of value 5 is added to this set, find the new values of the mean and the standard deviation.

4.	The mean, median and the standard deviation of a distribution are 28, 32 and 5, respectively. Calculate Karl Pearson's coefficient of skewness and describe the shape of the distribution.
4.	
4.	Calculate Karl Pearson's coefficient of skewness and describe the shape of the distribution.
4.	Calculate Karl Pearson's coefficient of skewness and describe the shape of the distribution. Is the mean a fair measurement of the central tendency for this distribution? Give reasons for
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5.	The speed of vehicles travelling on a certain section of a highway, is normally distributed with mean 90 km h^{-1} and standard deviation 10 km h^{-1} . Find the probability that the speed of a random selected vehicle is between 85 km h^{-1} and 100 km h^{-1} .
	······································
	It is found from previous records that 10% of the bolts produced by a machine are defective. If 5 bolts produced by this machine are chosen at random, find the probability that
	(i) exactly 3 bolts are defective, (ii) more than 2 bolts are non-defective .
	(i) exactly 3 bolts are defective,
	(i) exactly 3 bolts are defective,
	(i) exactly 3 bolts are defective,
	(i) exactly 3 bolts are defective,
	(i) exactly 3 bolts are defective,
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	(i) exactly 3 bolts are defective,
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	(i) exactly 3 bolts are defective,

7. In a group consisting of 30 cricketers, 20 have played for club A and 15 have play Every cricketer has played for at least one of these clubs. Find the probability t selected at random has played for club B , given that he has played for club A .	yed for club <i>B</i> . hat a cricketer
· · · · · · · · · · · · · · · · · · ·	
3. Let A and B be two events of a sample space S such that $P(A) = \frac{3}{8}$, $P(A \cap B) = \frac{1}{8}$ and	$P(A \cup B) = \frac{3}{2}$
Find	4
Find (i) $P(B)$, (ii) $P(A' \cap B)$ and (iii) $P(A' B)$.	4
Find	

0	The	probability	****	function	of	0	discrete	random	wariable	V	ic	given	helow
ン。	1116	probability	111222	Tuncuon	O1	a	arscrere	Talluolli	variable	Λ	13	grvcn	DCIOW.

х	1	2	3	4	5
P(X=x)	p	2p	p	2p	p

Find the value of the constant p and show that E(X) = 3.

Let Y be the random variable given by 3X-4. Find P(Y>X).

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10. A continuous random variable X has probability density function f(x) given by

$$f(x) = \begin{cases} kx - x^2 & , & \text{if } 0 \le x \le 1, \\ 0 & , & \text{otherwise}, \end{cases}$$

where k is a constant.

Show that $k = \frac{8}{3}$ and find E(X).

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கீයලු ම හිමිකම් ඇවිරිනි /முழுப் பதிப்புரிமையுடையது $|All\ Rights\ Reserved|$

(නව නිර්දේශය/புதிய பாடத்திட்டம்/New Syllabus)

eon විතාල දෙපාර්තමේන්තුව ලී ලංකා විතාල දෙපාර්තලේන්තුව කි. ඉ<mark>නු පිහිට දිනු පිහුර දුන් පිහුර දෙපාර්තමේන්තුව ලී ලංකා විතාල දෙපාර්තමේන්තුව නිශෝස්සභාව මුහෝසාසභාව වූ මා මා මෙන්නුවා ප්රධාන දෙපාර්තමේන්තුව ලී ලංකා විතාල දෙපාර්තමේන්තුව ලේකා විතාල දෙපාර්තමේන්තුව ලී ලංකා විතාල දෙපාර්තමේන්තුව ලේකා විතාල දෙපාර්තමේන් දෙපාර්තමේන්තුව ලේකා විතාල දෙපාර්තමේන්තුව ලේකා විතාල දෙපාර්තමේන් විතා</mark>

අධායන පොදු සහකික පතු (උසස් පෙළ) විභාගය, 2020 கல்விப் பொதுத் தராதரப் பத்திர (உயர் தர)ப் பரீட்சை, 2020 General Certificate of Education (Adv. Level) Examination, 2020

ගණිතය II සංක්ඛපුර II Mathematics II



Part B

- * Answer five questions only.
- 11. A factory manufactures tables and chairs. The production of each item requires three operations: cutting, assembling and finishing.

For cutting, assembling and finishing, the maximum number of hours that can be used are 600, 160 and 280, respectively. The following table gives the number of hours required for each operation in producing each item and the profit per item sold.

_		Number of hours for cutting	Number of hours for assembling	Number of hours for finishing	Profit (in thousands of rupees)
	Table	5	1	1	12
	Chair	6	2	4	15

The factory wishes to maximize the profit.

- (i) Formulate this as a linear programming problem.
- (ii) Sketch the feasible region.
- (iii) Using the graphical method, find the solution of the problem formulated in part (i) above.
- (iv) Due to shortage of storage space, the factory has to limit the total number of tables and chairs produced to at most 108. Find the decrease in the profit due to above limitation, if the factory still wishes to maximize the profit.

12.(a) Let
$$A = \begin{pmatrix} 4 & 7 \\ -1 & -2 \end{pmatrix}$$
. Write down A^{-1} .

Let
$$\mathbf{B} = \begin{pmatrix} -1 & 3 \\ 0 & 1 \end{pmatrix}$$
.

Find the matrix \mathbb{C} such that $A\mathbb{C} = \mathbb{B}$ and show that

$$\mathbf{AC} - \mathbf{CA} = \left(\begin{array}{cc} 20 & 43 \\ -11 & -20 \end{array} \right).$$

Find the matrix \mathbb{D} such that $AC - \mathbb{D}A = \mathbb{O}$, where \mathbb{O} is the zero matrix of order 2.

(b) Let $a \in \mathbb{R}$. Write the pair of simultaneous equations

$$(a-5)x + 3y = a$$

-4x + $(a + 2)y = 1$

in the form $\mathbb{P}\mathbb{X} = \mathbb{Q}$, where $\mathbb{X} = \begin{pmatrix} x \\ y \end{pmatrix}$, and \mathbb{P} and \mathbb{Q} are matrices to be determined.

Express
$$\Delta = \begin{vmatrix} (a-5) & 3 \\ -4 & (a+2) \end{vmatrix}$$
 as a quadratic function of a .

Show that the roots of the equation $\Delta = 0$ are a = 1 and a = 2.

- Show that the above pair of equations has
 - (i) infinitely many solutions when a = 1,
 - (ii) no solution when a = 2,
 - (iii) a unique solution when a = 3.
- 13.(a) An unbiased cubic die with faces marked 1, 2, 2, 3, 3, 4 is tossed twice. Let A be the event that the sum of the numbers obtained is 4 and B be the event that the sum of the numbers obtained is even.

Find P(A), P(B) and $P(A \mid B)$.

- (b) Four digits from the set of digits {1, 2, 3, 4, 5, 6} are chosen without replacement and a 4-digit number is made.
 - (i) How many different 4-digit numbers can be made?
 - (ii) How many of these 4-digit numbers start with 3 or 5?
- (c) A team of four people must be selected from a group of four males and two females.
 - (i) How many different teams of four people can be selected?
 - (ii) Find the probability that both females are selected to these teams.
- 14. A box X contains 4 red cards and 6 blue cards. A box Y contains 3 red cards and 2 blue cards. A biased coin with $\frac{2}{3}$ as the probability of getting a head is tossed. If the outcome is a head, 2 cards are drawn from the box X, at random without replacement, and if it is a tail, 2 cards are drawn from the box Y, at random without replacement. Find the probability that
 - (i) both cards drawn are red,
 - (ii) at least one of the cards drawn is red,
 - (iii) the two cards drawn are of different colours,
 - (iv) the two cards drawn are of different colours, given that at least one of the cards drawn is red.

15.(a) The time X, measured in minutes, between consecutive arrivals of buses to a certain bus stop is exponentially distributed with probability density function

$$f(x) = \begin{cases} \lambda e^{-\lambda x} &, & x > 0, \\ 0 &, & \text{otherwise,} \end{cases}$$

where λ (> 0) is a parameter.

If the mean number of buses that arrive at the bus stop in an hour is 12, find the value of λ .

- (i) After a bus arrives at the bus stop, find the probability that the time taken for the next bus to arrive at the bus stop is
 - (α) between one minute to three minutes,
 - (β) less than five minutes.
- (ii) If it is given that five minutes has already passed from the arrival of a bus to the bus stop, find the probability that it takes at least an additional two minutes for the next bus to arrive.
- (b) A continuous random variable X is uniformly distributed over the interval [a, b].

Find the values of a and b such that P(X < 16) = 0.4 and P(X > 21) = 0.2.

16. Hundred students faced an entrance test. The frequency distribution of the marks they obtained is given in the following table:

Marks	frequency
0 – 20	15
20 – 40	20
40 – 60	40
60 – 80	15
80 – 100	10

- (i) Estimate each of the following:
 - (a) the mean,
 - (b) the standard deviation,
 - (c) the median,
 - (d) the inter quartile range and
 - (e) the mode

of the marks.

(ii) After rescrutiny, it was discovered that the marks of two answer scripts should be changed as follows:

Marks before	Marks after
rescrutiny	rescrutiny
50	62
70	75

Find the mean of the new distribution of marks.

17. The duration of activities of a project and the flow of activities are given in the following table:

Activity	Preceding Activity (Activities)	Duration (in Weeks)
A	_	03
В	A	08
С	A	05
D	A	03
Е	В	06 .
F	С	03
G	E, F	04
Н	D, F	06
I	G, H	03 .

- (i) Construct the project network.
- (ii) Prepare an activity schedule that includes earliest start time, earliest finish time, latest start time, latest finish time and float for each activity.
- (iii) Find the total duration of the project.
- (iv) What are the activities that can be delayed without extending the total duration of the project?
- (v) Write down the critical path of this project.
- (vi) Suppose that the duration of the activity D has to be extended by two weeks due to an unexpected matter. Determine whether the project could still be completed within the total duration calculated in part (iii) above.